

Compiler Construction (CS-636)

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(Week 11) Lecture 21 & 22

Objectives: Learning objectives of these lectures are

Students will be able to understand:

- What is Bottom-Up Parser?
- What are types of Bottom-Up Parser?
- CLR(1) Parser Steps
 1. Number the Production
 2. Augment the given grammar (Augmented Grammar)
 3. Draw the Canonical Collection
 4. Create the Parsing Table
 5. Stack Implementation
 6. Draw Parse Tree

Text Book & Resources:

Compilers Principles Techniques and Tools (2nd Edition) by Alfred V. Aho, Ravi Sethi.

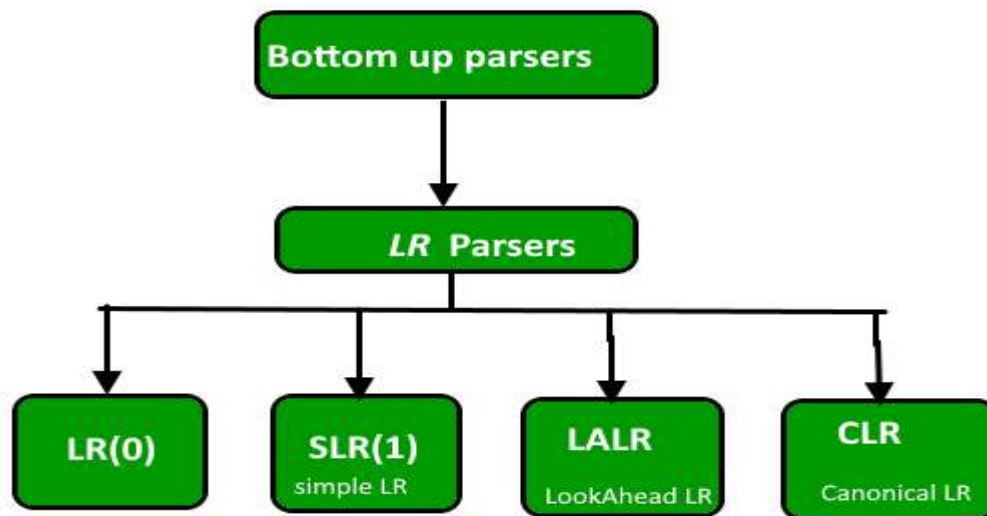
Videos Links:

https://youtu.be/OFSM7gV66zE	(Part 1)
https://youtu.be/GapyvMhJdDU	(Part 2)
https://youtu.be/F64pAwqDqQ4	(Part 3)
https://youtu.be/iduYikgpcNE	(Part 4)
https://youtu.be/Gf5vvA0k21k	(Part 5)
https://youtu.be/Ctl6A4p9SEo	(Part 6)
https://youtu.be/cyYZuL2GELk	(Part 7)
https://youtu.be/1Nr58CngFwY	(Part 8)

Bottom Up or Shift Reduce Parsers

In the last week, we had discussed the Bottom Up Parsers and also discussed the following types of parsers. From these parsers we had discussed SLR(1) Parser and in this week we will discuss the Canonical LR or CLR(1) Parser.

Classification (Types) of bottom up parsers



CLR (1) Parsing

CLR refers to canonical look-ahead. CLR parsing use the canonical collection of LR (1) items to build the CLR(1) parsing table. CLR (1) parsing table produces the more number of states as compare to the SLR (1) parsing.

In the CLR (1), we place the reduce node only in the look-ahead symbols.

Canonical LR Parsing

Algorithm:

```

SetOfItems CLOSURE( $I$ ) {
    repeat
        for ( each item  $[A \rightarrow \alpha \cdot B \beta, a]$  in  $I$  )
            for ( each production  $B \rightarrow \gamma$  in  $G'$  )
                for ( each terminal  $b$  in  $\text{FIRST}(\beta a)$  )
                    add  $[B \rightarrow \cdot \gamma, b]$  to set  $I$ ;
    until no more items are added to  $I$ ;
    return  $I$ ;
}
    
```

```

SetOfItems GOTO( $I, X$ ) {
    initialize  $J$  to be the empty set;
    for ( each item  $[A \rightarrow \alpha \cdot X \beta, a]$  in  $I$  )
        add item  $[A \rightarrow \alpha X \cdot \beta, a]$  to set  $J$ ;
    return CLOSURE( $J$ );
}

void items( $G'$ ) {
    initialize  $C$  to CLOSURE( $\{[S' \rightarrow \cdot S, \$]\}$ );
    repeat
        for ( each set of items  $I$  in  $C$  )
            for ( each grammar symbol  $X$  )
                if ( GOTO( $I, X$ ) is not empty and not in  $C$  )
                    add GOTO( $I, X$ ) to  $C$ ;
    until no new sets of items are added to  $C$ ;
}

```

Construction of Canonical LR Parsing Table

Algorithm:

1. Construct $C' = \{I_0, I_1, \dots, I_n\}$, the collection of sets of LR(1) items for G' .
2. State i of the parser is constructed from I_i . The parsing action for state i is determined as follows.
 - (a) If $[A \rightarrow \alpha \cdot a \beta, b]$ is in I_i and $\text{GOTO}(I_i, a) = I_j$, then set $\text{ACTION}[i, a]$ to "shift j ." Here a must be a terminal.
 - (b) If $[A \rightarrow \alpha \cdot, a]$ is in I_i , $A \neq S'$, then set $\text{ACTION}[i, a]$ to "reduce $A \rightarrow \alpha$."
 - (c) If $[S' \rightarrow S \cdot, \$]$ is in I_i , then set $\text{ACTION}[i, \$]$ to "accept."

If any conflicting actions result from the above rules, we say the grammar is not LR(1). The algorithm fails to produce a parser in this case.

3. The goto transitions for state i are constructed for all nonterminals A using the rule: If $\text{GOTO}(I_i, A) = I_j$, then $\text{GOTO}[i, A] = j$.
4. All entries not defined by rules (2) and (3) are made "error."
5. The initial state of the parser is the one constructed from the set of items containing $[S' \rightarrow \cdot S, \$]$.

CLR(1) Parser Steps

1. Number the Production
2. Augment the given grammar (Augmented Grammar)
3. Draw the Canonical Collection (DFD)
4. Create the Parsing Table
5. Stack Implementation
6. Draw Parse Tree

Example # 1

Consider the grammar

$S \rightarrow AA$

$A \rightarrow aA \mid b$

Step 1: Number the Production

1. $S \rightarrow AA$
2. $A \rightarrow aA$
3. $A \rightarrow b$

Step 2: Augmented CFG

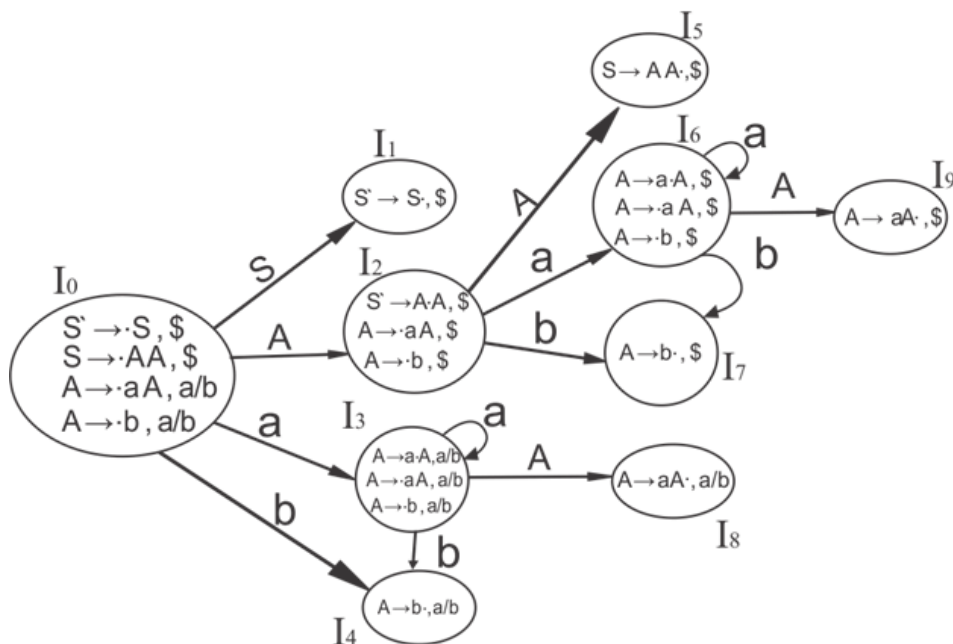
$S' \rightarrow S$

$S \rightarrow AA$

$A \rightarrow aA$

$A \rightarrow b$

Step 3: Canonical Collection



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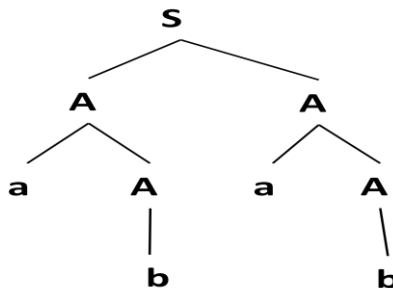
Step 4: Parsing Table (R1: $S \rightarrow AA$, R2: $A \rightarrow aA$, R3: $A \rightarrow b$)

States	Action Part			Goto Part	
	a	b	\$	S	A
I ₀	S3	S4		1	2
I ₁			Accept		
I ₂	S6	S7			5
I ₃	S3	S4			8
I ₄	R3	R3			
I ₅			R1		
I ₆	S6	S7			9
I ₇			R3		
I ₈	R2	R2			
I ₉			R2		

Step 5: Stack Implementation (String: **abab**)

Stack	Input	Action
\$0	abab\$	Shift $a \rightarrow S3$
\$0a3	bab\$	Shift $b \rightarrow S4$
\$0a3b4	ab\$	Reduction ($A \rightarrow b$) (R3)
\$0a3A8	ab\$	Reduction ($A \rightarrow aA$) (R2)
\$0A2	ab\$	Shift $a \rightarrow S6$
\$0A2a6	b\$	Shift $b \rightarrow S7$
\$0A2a6b7	\$	Reduction ($A \rightarrow b$) (R3)
\$0A2a6A9	\$	Reduction ($A \rightarrow aA$) (R2)
\$0A2A5	\$	Reduction ($S \rightarrow AA$) (R1)
\$0S1	\$	Accept

Step 6: Draw Syntax Tree



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Example # 2

Given Grammar

$S \rightarrow (S) \mid \epsilon$

Step # 1: Number the Production

1. $S \rightarrow (S)$

2. $S \rightarrow \epsilon$

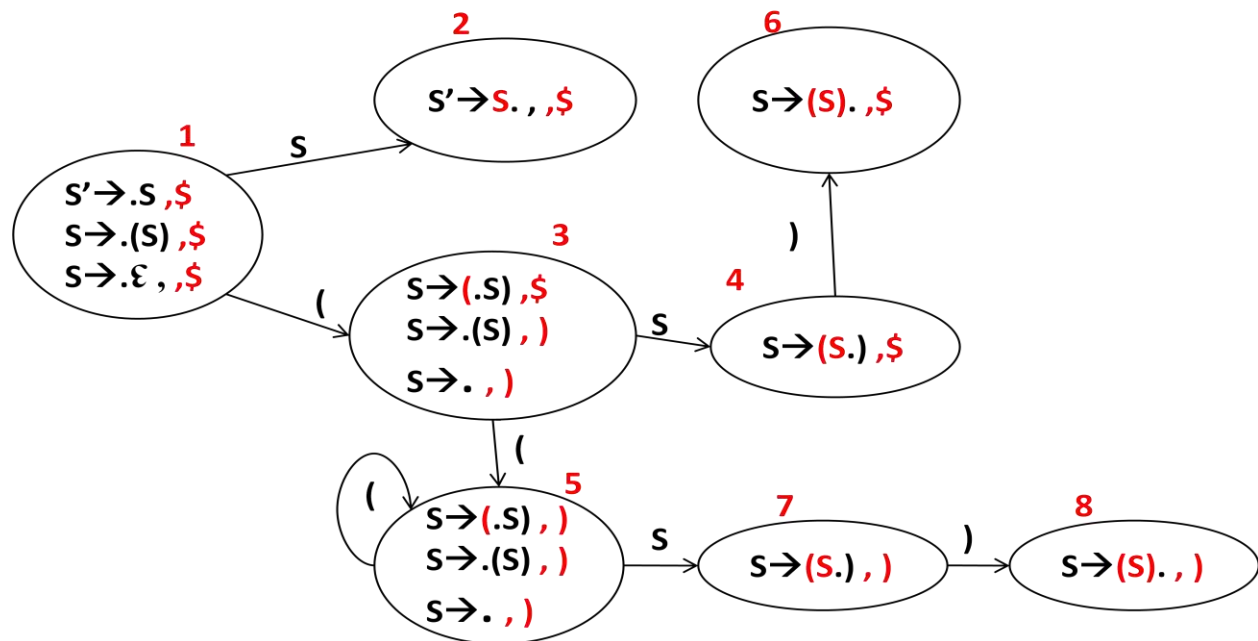
Step # 2: Augmented Grammar

$S' \rightarrow S$

$S \rightarrow (S)$

$S \rightarrow \epsilon$

Step 3: Canonical Collection



Note: $S \rightarrow \epsilon = S \rightarrow \cdot$ so there is to need to check next symbol

Step 4: Parsing Table (R1: $S \rightarrow (S)$, R2: $S \rightarrow \epsilon$)

States	Action Part			Goto Part
	(	)	\$	S
1	S3		R2	2
2			Accept	
3	S5	R2		4
4		S6		
5	S5	R2		7
6			R1	
7		S8		
8		R1		

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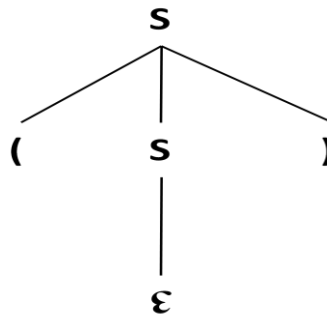
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Step 5: Stack Implementation (String: ())

Stack	Input	Action
\$1	()\$	Shift ($\rightarrow S3$)
\$1(3	)\$	Reduction ($S \rightarrow \epsilon$ (R2))
\$1(3S4	)\$	Shift ($\rightarrow S6$)
\$1(3S4)6	\$	Reduction ($S \rightarrow (S)$ (R1))
\$1S2	\$	Accept

Step 6: Draw Syntax Tree



Example # 3

In this example we will perform all above steps to check whether the given grammar is CLR(1) conflict or not.

Given CFG:

$E \rightarrow E+(E)$

$E \rightarrow id$

Given String:

$id+(id)$

Step 1: Number the Production

1. $E \rightarrow E+(E)$

2. $E \rightarrow id$

Step 2: Augmented CFG

$E' \rightarrow E$

$E \rightarrow E+(E)$

$E \rightarrow id$

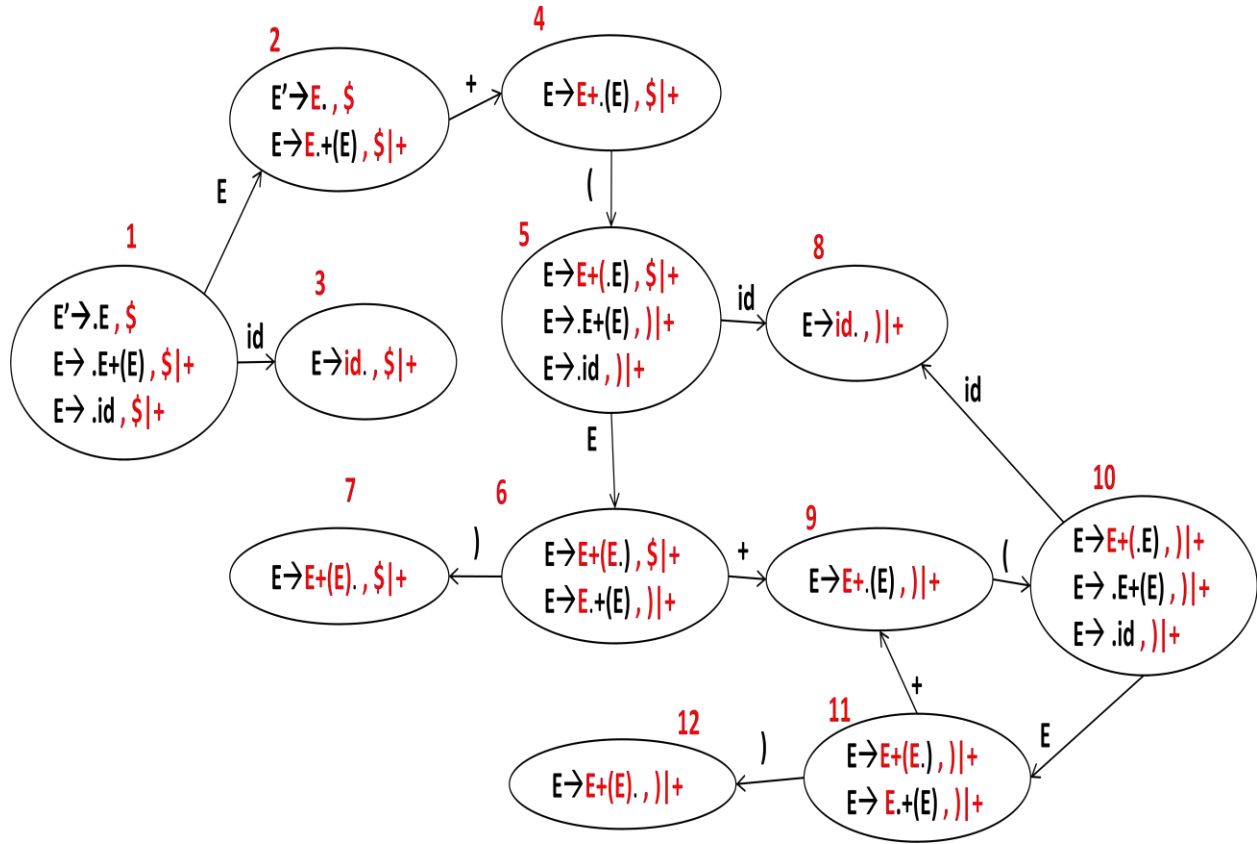
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Step 3: Canonical Collection



Step 4: Parsing Table (R1: $E \rightarrow E+(E)$, R2: $E \rightarrow id$)

States	Action Part					Goto Part
	+	(	id	)	\$	
1			S3			2
2	S4				Accept	
3	R2				R2	
4		S5				
5			S8			6
6	S9			S7		
7	R1				R1	
8	R2			R2		
9		S10				
10			S8			11
11	S9			S12		
12	R1			R1		

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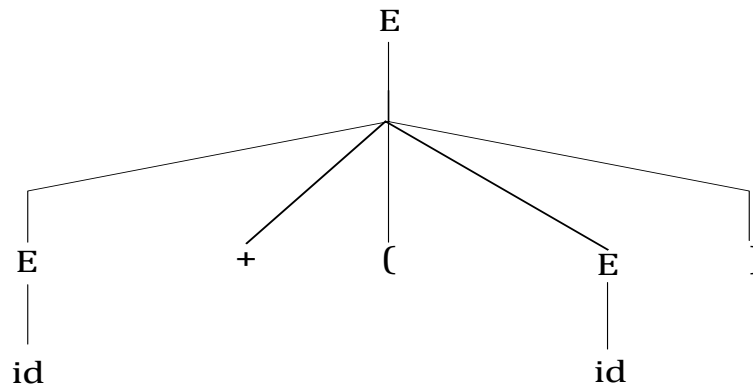
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Step 5: Stack Implementation (String: **id+(id)**)

Stack	Input	Action
\$1	id+(id)\$	Shift id → S3
\$1id3	+(id)\$	Reduction (E → id) (R2)
\$1E2	+(id)\$	Shift + → S4
\$1E2+4	(id)\$	Shift (→ S5
\$1E2+4(5	id)\$	Shift id → S8
\$1E2+4(5id8	)\$	Reduction E → id (R2)
\$1E2+4(5E6	)\$	Shift) → S7
\$1E2+4(5E6)7	\$	Reduction E → E+(E) (R1)
\$1E2	\$	Accept

Step 6: Draw Syntax Tree



Example # 4

Given CFG

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow id$

In this example we will perform all above steps to check whether the given grammar is CLR(1) conflict or not.

Step 1: Number the Production

1. $E \rightarrow E + T$

2. $E \rightarrow T$

3. $T \rightarrow T * F$

4. $T \rightarrow F$

5. $F \rightarrow id$

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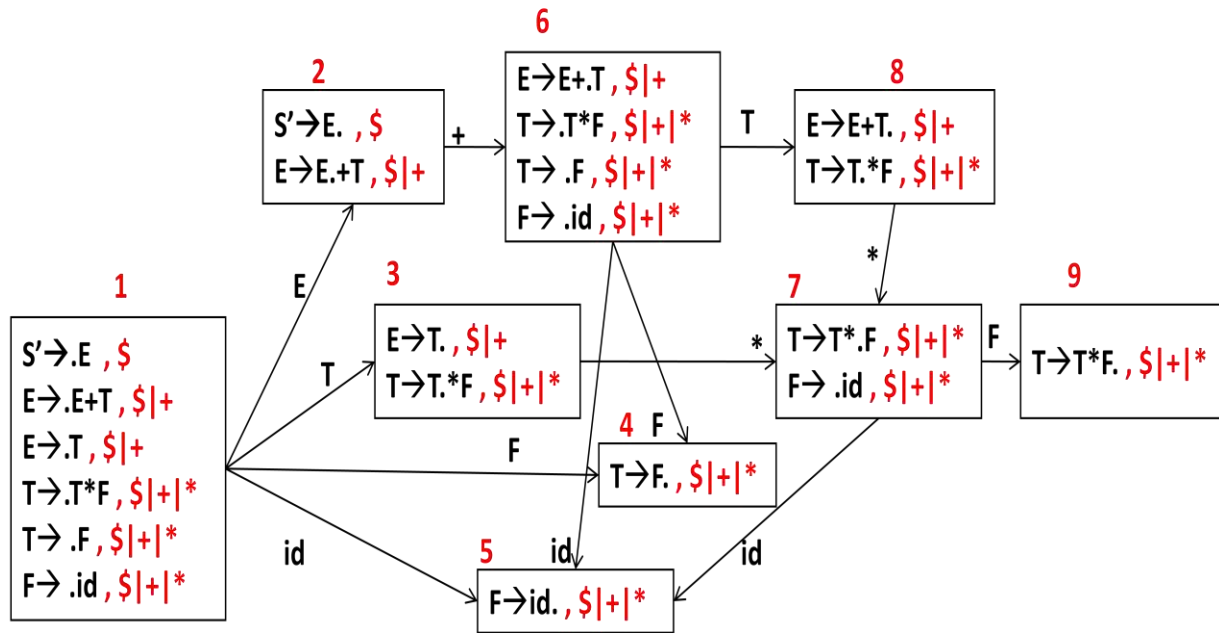
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Step 2: Augmented CFG

$S' \rightarrow E$
 $E \rightarrow E + T$
 $E \rightarrow T$
 $T \rightarrow T * F$
 $T \rightarrow F$
 $F \rightarrow id$

Step 3: Canonical Collection (DFD)



Step 4: Parsing Table (R1: $E \rightarrow E+T$, R2: $E \rightarrow T$, R3: $T \rightarrow T*F$, R4: $T \rightarrow F$, R5: $F \rightarrow id$)

States	Action Part				Goto Part		
	id	+	*	\$	E	T	F
1	S5				2	3	4
2		S6		Accept			
3		R2	S7	R2			
4		R4	R4	R4			
5		R5	R5	R5			
6	S5					8	4
7	S5						9
8		R1	S7	R1			
9		R3	R3	R3			

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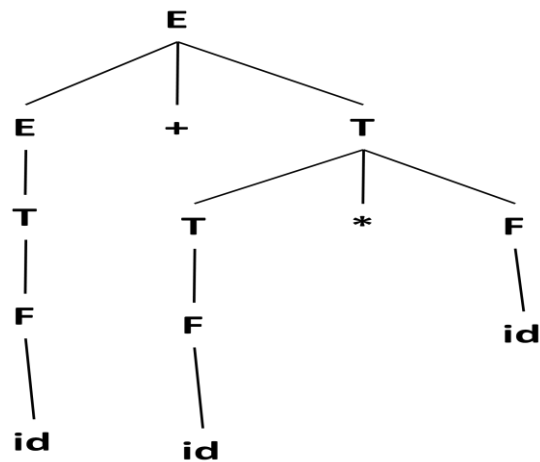
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Step 5: Stack Implementation (String: **id+id*id**)

Stack	Input	Action
\$1	id+id*id\$	Shift id →S5
\$1id5	+id*id\$	Reduction (F →id) (R5)
\$1 F 4	+id*id\$	Reduction (T →F) (R4)
\$1 T 3	+id*id\$	Reduction (E →T) (R2)
\$1 E 2	+id*id\$	Shift + →S6
\$1E2+6	id*id\$	Shift id →S5
\$1E2+6id5	*id\$	Reduction (F →id) (R5)
\$1E2+6 F 4	*id\$	Reduction (T →F) (R4)
\$1E2+6 T 8	*id\$	Shift * →S7
\$1E2+6T8*7	id\$	Shift id →S5
\$1E2+6T8*7id5	\$	Reduction (F →id) (R5)
\$1E2+6T8*7 F 9	\$	Reduction (T →T*F) (R3)
\$1E2+6T8	\$	Reduction (E →E+T) (R1)
\$1 E 2	\$	Accept

Step 6: Draw Syntax Tree



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Example # 5

Given Grammar

$S \rightarrow SS+ \mid SS* \mid a$

Step # 1: Number the Production

1. $S \rightarrow SS+$
2. $S \rightarrow SS*$
3. $S \rightarrow a$

Step # 2: Augmented Grammar

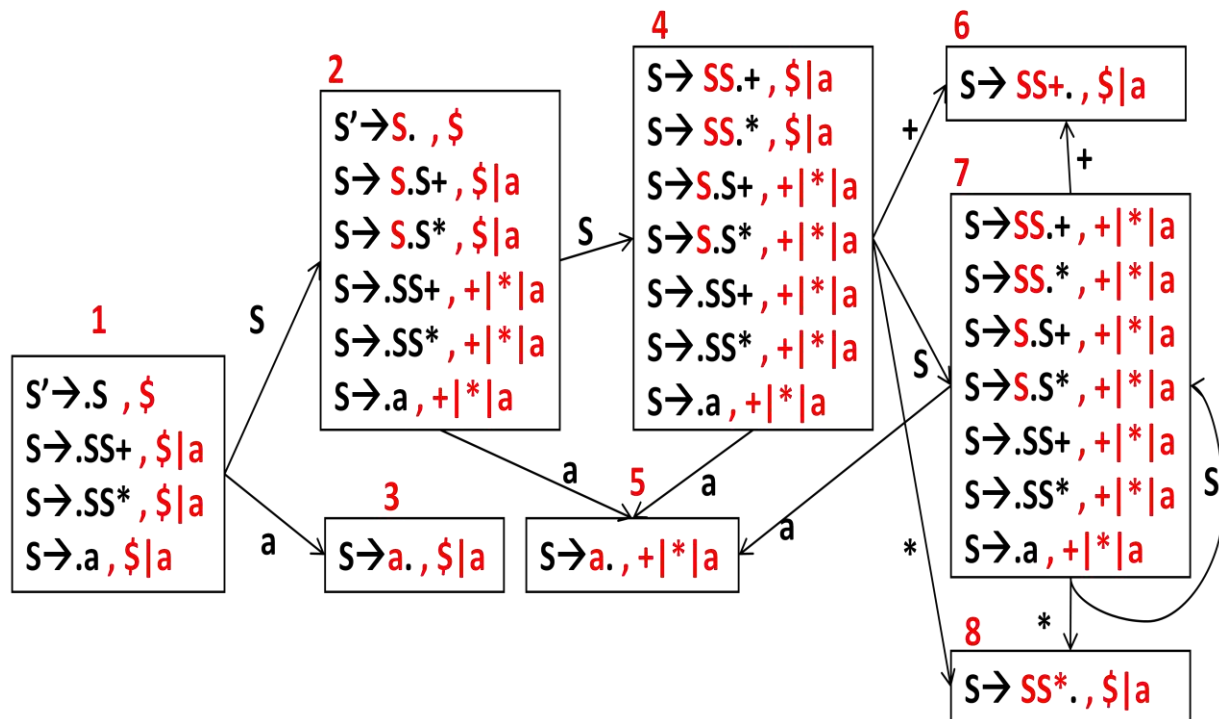
$S' \rightarrow S$

$S \rightarrow SS+$

$S \rightarrow SS*$

$S \rightarrow a$

Step 3: Canonical Collection of LR(1) Items



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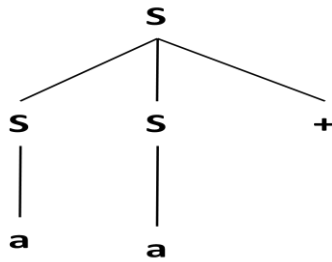
Step 4: Parsing Table (R1: $S \rightarrow SS+$, R2: $S \rightarrow SS^*$, R3: $S \rightarrow a$)

States	Action Part				GoTo Part
	+	*	a	\$	S
1			S3		2
2			S5	Accept	4
3			R3	R3	
4	S6	S8	S5		7
5	R3	R3	R3		
6			R1	R1	
7	S6	S8	S5		7
8			R2	R2	

Step5: Stack Implementation (String: aa^+)

Stack	Input	Action
\$1	aa+\$	Shift $a \rightarrow S3$
\$1a3	a+\$	Reduction $R3(S \rightarrow a)$
\$1S2	a+\$	Shift $a \rightarrow S5$
\$1S2a5	+\$	Reduction $R3(S \rightarrow a)$
\$1S2S4	+\$	Shift $+ \rightarrow S6$
\$1S2S4+6	\$	Reduction $R1(S \rightarrow SS+)$
S1S2	\$	Accept

Step 6: Draw Syntax Tree



Example # 6

Given Grammar

$S \rightarrow (L) \mid a$

$L \rightarrow L, S \mid S$

Step # 1: Number the Production

1. $S \rightarrow (L)$
2. $S \rightarrow a$
3. $L \rightarrow L, S$
4. $L \rightarrow S$

Step # 2: Augmented Grammar

$S' \rightarrow S$

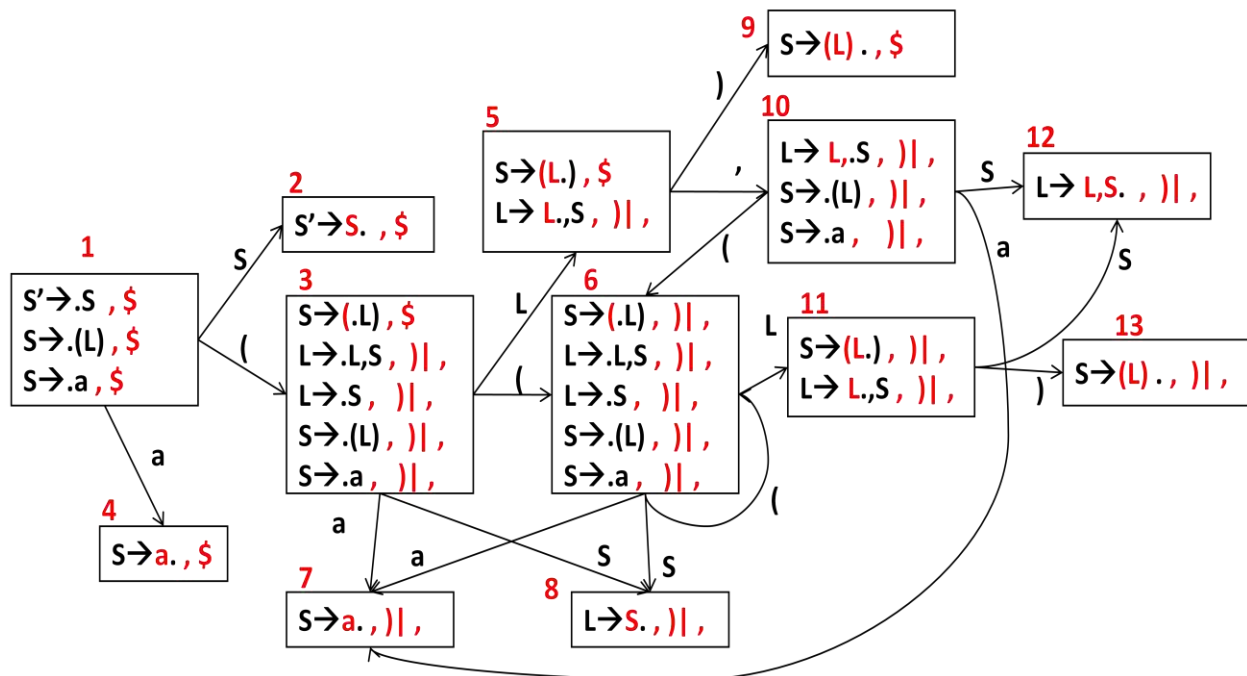
$S \rightarrow (L)$

$S \rightarrow a$

$L \rightarrow L, S$

$L \rightarrow S$

Step 3: Canonical Collection



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Step 4: Parsing Table (R1: $S \rightarrow (L)$, R2: $S \rightarrow a$, R3: $L \rightarrow L,S$, R4: $L \rightarrow S$)

States	Terminal Part					Goto Part	
	(	)	a	,	\$	S	L
1	S3		S4			2	
2					Accept		
3	S6		S7			8	5
4					R2		
5		S9		S10			
6	S6		S7			8	11
7		R2		R2			
8		R4		R4			
9					R1		
10	S6		S7			12	
11		S13				12	
12		R3		R3			
13		R1		R1			

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Step 5 : Stack Implementation (**String: (a,a)**)

Stack	Input	Action
\$1	(a , a)\$	Shift $(\rightarrow S3$
\$1(3	a , a)\$	Shift $a \rightarrow S7$
\$1(3a7	,a)\$	Reduction $R2(S \rightarrow a)$
\$1(3S8	,a)\$	Reduction $R4(L \rightarrow S)$
\$1(3L5	,a)\$	Shift $, \rightarrow S10$
\$1(3L5,10	a)\$	Shift $a \rightarrow S7$
\$1(3L5,10a7	)\$	Reduction $R2(S \rightarrow a)$
\$1(3L5,10S12	)\$	Reduction $R3(L \rightarrow L,S)$
\$1(3L5	)\$	Shift $) \rightarrow S9$
\$1(3L5)9	\$	Reduction $R1(S \rightarrow (L)$
\$1S2	\$	Accept

Step 6: Draw Syntax Tree

